

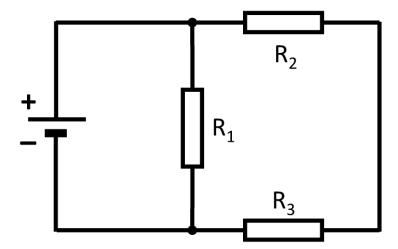
Kirchhoff's Circuit Laws

Electrical Engineering
Wolfgang Neff



Kirchhoff's Circuit Laws (1)

- Complex Circuits
 - Are completely described by current and voltage
 - The junctions tell us something about current
 - The loops tell us something about voltage





Kirchhoff's Circuit Laws (2)

- Calculation of Unknown Circuit Quantities
 - Make a list of all known values
 - 2. Mark all currents and voltages including arrows
 - 3. Write down the equations for all junctions and loops
 - 4. Set up the equations for all resistors
 - 5. Set up the linear system of equations and solve it





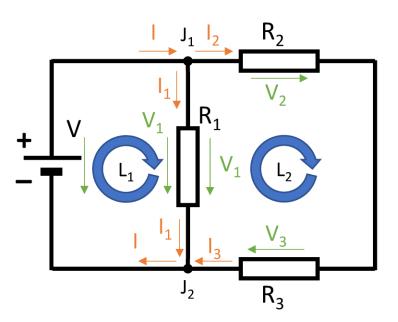
Kirchhoff's Circuit Laws (3)

Example

- Make a list of all known values
- Mark all currents and voltages including arrows

Known Values:

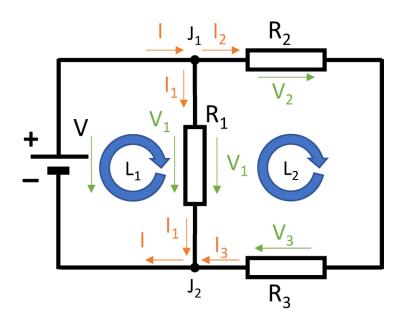
- V = 5 V
- $R_1 = 200 \Omega$
- $R_2 = 100 \Omega$
- $R_3 = 50 \Omega$





Kirchhoff's Circuit Laws (4)

- Example (continued)
 - Write down the equations for all junctions and loops



Meshes:

- $V_1 V = 0$
- $V_1 + V_2 V = 0$
- $V_2 + V_3 V_1 = 0$

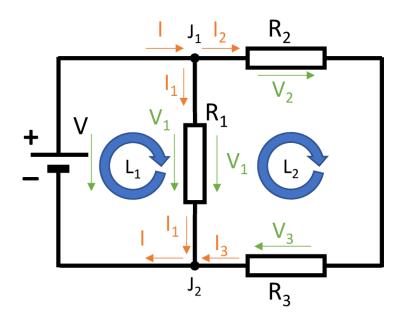
Junctions:

- $I I_1 I_2 = 0$
- $I_1 + I_3 I = 0$



Kirchhoff's Circuit Laws (5)

- Example (continued)
 - Set up the equations for all resistors



Resistors:

- $V_1 = R_1 \cdot I_1$
- $V_2 = R_2 \cdot I_2$
- $V_3 = R_3 \cdot I_3$



Kirchhoff's Circuit Laws (6)

- Example (continued)
 - Set up the linear system of equations

Known Values:

- V = 5 V
- $R_1 = 200 \Omega$
- $R_2 = 100 \Omega$
- $R_3 = 50 \Omega$

Meshes:

System of Equations

•
$$V_1 - V = 0$$
 $\rightarrow V_1 = 5$

•
$$V_1 + V_2 - V = 0 \rightarrow V_1 + V_2 = 5$$

•
$$V_2 + V_3 - V_1 = 0 \rightarrow -V_1 + V_2 + V_3 = 0$$

Junctions:

•
$$I - I_1 - I_2 = 0$$
 \rightarrow $J - J_1 - J_2 = 0$

•
$$I_1 + I_3 - I = 0$$
 \Rightarrow $J_1 + J_3 - J = 0$

Resistors:

•
$$V_1 = R_1 \cdot I_1$$
 $\rightarrow V_1 - 200 J_1 = 0$
• $V_2 = R_2 \cdot I_2$ $\rightarrow V_2 - 100 J_2 = 0$

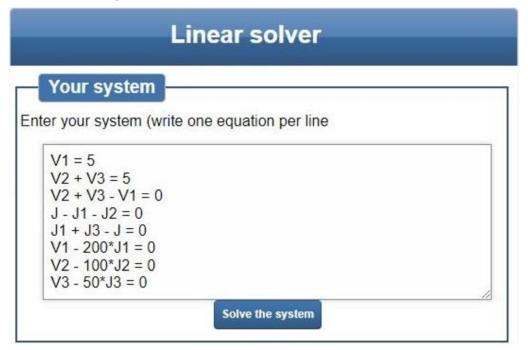
$$V_2 = R_2 \cdot I_2$$
 $\rightarrow V_2 - 100 J_2 = 0$

•
$$V_3 = R_3 \cdot I_3$$
 $\rightarrow V_3 - 50 J_3 = 0$



Kirchhoff's Circuit Laws (7)

- Example (continued)
 - Provide the equations to a linear solver



Source: https://wims.univ-cotedazur.fr/wims/wims.cgi?module=tool/linear/linsolver.en



Kirchhoff's Circuit Laws (8)

- Example (continued)
 - Solve the linear system of equations

Linear solver

You have entered the system

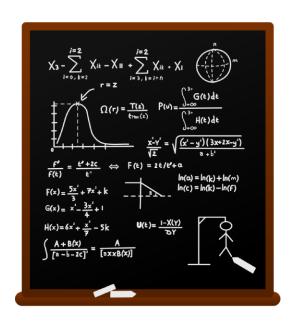
Source: https://wims.univ-cotedazur.fr/wims/wims.cgi?module=tool/linear/linsolver.en

1 This system has a unique solution, which is: j = 7/120, j1 = 1/40, j2 = 1/30, j3 = 1/30, v1 = 5, v2 = 10/3, v3 = 5/3



Kirchhoff's Circuit Laws (9)

- Example (finished)
 - V = 5 V
 - $V_1 = 5 V$
 - $V_2 = 3.33 \text{ V}$
 - $V_3 = 1.67 \text{ V}$
 - I = 58.33 mA
 - $I_1 = 25 \text{ mA}$
 - $I_2 = 33.33 \text{ mA}$



All currents and voltages are determined